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Abstract: Let M_n be the number of lattice paths in \mathbb{Z}^2/n connecting the origin with $(1, a)$ (to within $1/n$ roundoff error at the end) that never cross above the barrier curve $y(x)$. If $y(0)=0$, $y(1)=a$, and y is convex, then

$$\lim_{n \rightarrow \infty} \frac{1}{n} \log M_n = \int_0^1 (1+y'(x)) H(1/(1+y'(x))) dx,$$

where $H(p) = -(p \log p + (1-p) \log (1-p))$ is the usual entropy function; a slightly more complicated formula holds for non-convex barrier functions.